

A DYNAMICAL MODEL OF IMMUNE RESPONSE BY T CELLS

Alberto A. Pinto^{1,2*}, Bruno M. P. M. Oliveira^{2,3},
Isabel P. Figueiredo^{2,4}, and Nigel J. Burroughs⁵

¹Departamento de Matemática, Faculdade de Ciências da Universidade do Porto,
R. do Campo Alegre 687, 4169-007 Porto, Portugal.

²LIAAD - INESC Tec Porto, R. Dr. Roberto Frias, 4250-465 Porto, Portugal.

³Faculdade de Ciências da Nutrição e Alimentação da Universidade do Porto,
R. Dr. Roberto Frias, 4250-465 Porto, Portugal.

⁴Instituto Superior de Engenharia do Porto,
R. Dr. António Bernardino de Almeida, 431, 4200-072 Porto, Portugal.

⁵Mathematics Institute and Warwick Systems Biology Centre,
University of Warwick, Coventry. CV4 7AL. UK.

aapinto1@gmail.com (*corresponding author)

ABSTRACT

We analyse a model of immune response by T cells (CD4), where regulatory T cells (Tregs) act by inhibiting IL-2 secretion. We introduced an asymmetry reflecting that the difference between the growth and death rates can be higher for the active T cells and the active Tregs than for the inactive T cells and inactive Tregs. We present an explicit formula that gives the approximate balance between the antigenic stimulation of T cells and the concentration of Tregs. Furthermore, we present an explicit formula that relates approximately the antigenic stimulation of T cells, the concentration of T cells and the concentration of Tregs. For our parameter values, the relation between the antigenic stimulation of T cells and the concentration of T cells is an hysteresis that is unfold when some of the parameters are changed. Moreover, when considering a linear tuning between the antigenic stimulation of T cells and the antigenic stimulation of Tregs, we were also able to obtain an explicit formula relating approximately the antigenic stimulation of T cells, the concentration of T cells and the concentration of Tregs. With it, we can explain the appearance of an isola and a transcritical bifurcation in the original hysteresis.